Graph of f
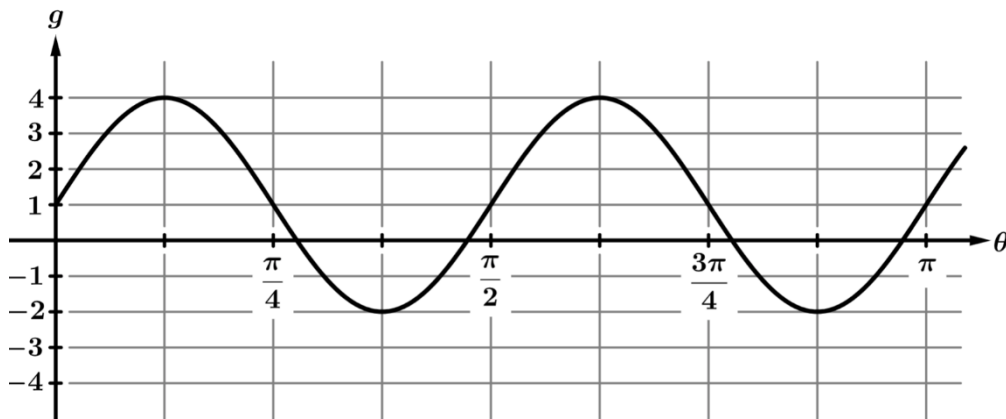
1. The sinusoidal function $f(x)$ is shown in the figure above. Find the period, frequency, amplitude, and midline for the graph of $f(x)$.

Period: **Frequency:**   **Midline:**   **Amplitude:**
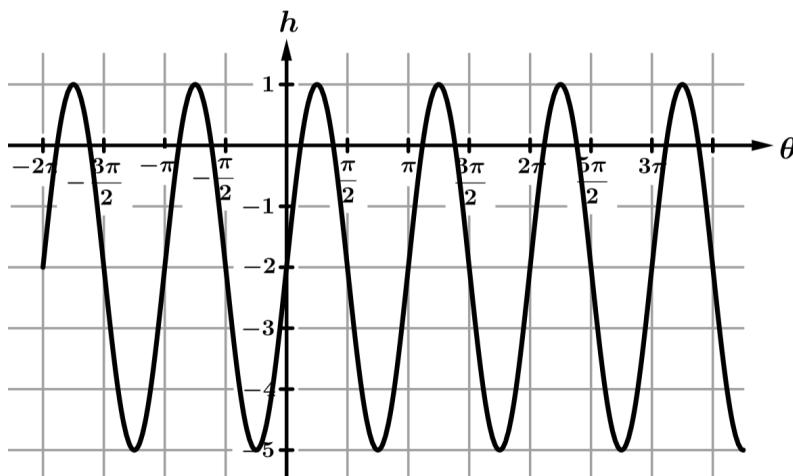

Graph of g

2. The sinusoidal function $g(\theta)$ is shown in the figure above. Find the period, frequency, amplitude, and midline for the graph of $g(\theta)$.

Period: **Frequency:**   **Midline:**   **Amplitude:**

Graph of h

3. The sinusoidal function $h(\theta)$ is shown in the figure above. Find the period, frequency, amplitude, and midline for the graph of $h(\theta)$.

Period: **Frequency:**   **Midline:**   **Amplitude:**

4. The sinusoidal function $g(\theta)$ has a maximum at the point $(0, 24)$. The first minimum after reaching this maximum value occurs at the point $(3\pi, 10)$. Find the period, frequency, amplitude, and midline for the graph of $g(\theta)$.

Period: **Frequency:**   **Midline:**   **Amplitude:**

5. The sinusoidal function $h(\theta)$ has a minimum at the point $\left(\dfrac{\pi}{4}, 6\right)$. The first maximum after reaching this minimum

value occurs at the point $\left(\dfrac{5\pi}{4}, 16\right)$. Find the period, frequency, amplitude, and midline for the graph of $h(\theta)$.

Period: **Frequency:**   **Midline:**   **Amplitude:**
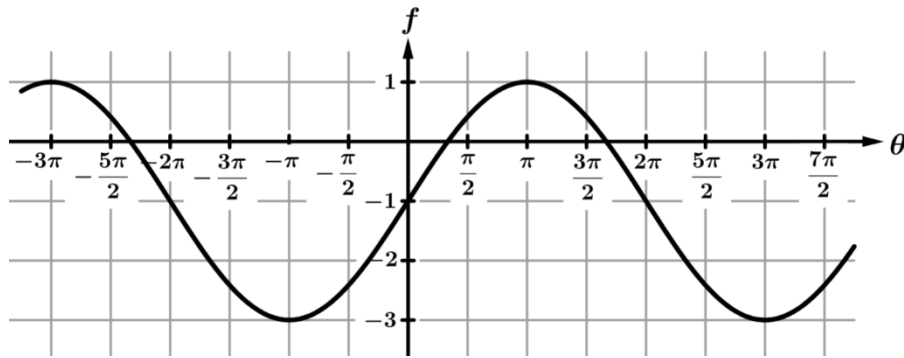
6. The sinusoidal function $k(\theta)$ has a minimum at the point $\left(-\dfrac{\pi}{2}, -4\right)$. The first maximum after reaching this minimum

value occurs at the point $(0, 8)$. Find the period, frequency, amplitude, and midline for the graph of $k(\theta)$.

Period: **Frequency:**   **Midline:**   **Amplitude:**

Directions: Use the graph of the sinusoidal function $f(\theta)$ to answer problems 7 – 10.


Graph of f

7. Which of the following best describes the behavior of f over the interval $0 < \theta < \pi$?

(A) f is increasing at an increasing rate.

(B) f is increasing at a decreasing rate.

(C) f is decreasing at an increasing rate.

(D) f is decreasing at a decreasing rate.

8. Which of the following best describes the behavior of f over the interval $-2\pi < \theta < -\pi$?

(A) f is increasing and the graph of f is concave up.

(B) f is increasing and the graph of f is concave down.

(C) f is decreasing and the graph of f is concave up.

(D) f is decreasing and the graph of f is concave down.

9. Which of the following best describes the behavior of f over the interval $2\pi < \theta < 3\pi$?

(A) f is positive and increasing.

(B) f is positive and decreasing.

(C) f is negative and increasing.

(D) f is negative and decreasing.

10. Which of the following best describes the rate of change of f over the interval $-\pi < \theta < 0$?

(A) The rate of change of f is positive and increasing.

(B) The rate of change of f is positive and decreasing.

(C) The rate of change of f is negative and increasing.

(D) The rate of change of f is negative and decreasing.

Directions: Use the graph of the sinusoidal function $g(\theta)$ to answer problems 11 – 14.
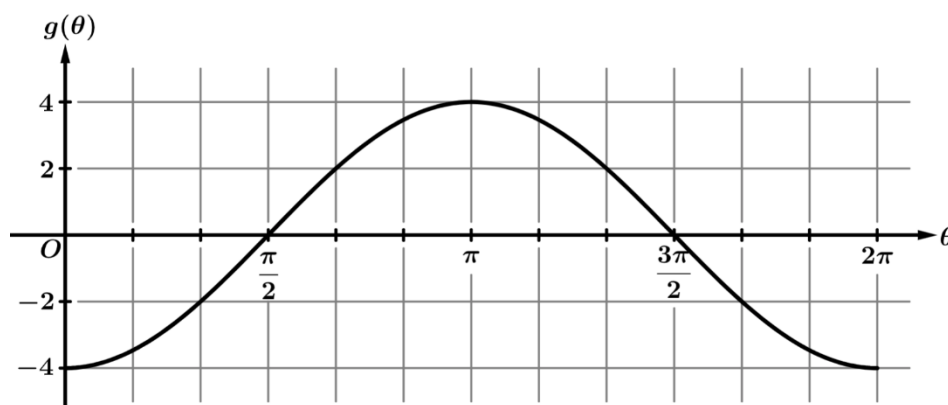
Graph of g

11. Which of the following best describes the behavior of g over the interval $0 < \theta < \dfrac{\pi}{2}$?

(A) g is positive and increasing.

(B) g is positive and decreasing.

(C) g is negative and increasing.

(D) g is negative and decreasing.

12. Which of the following best describes the behavior of g over the interval $\dfrac{\pi}{2} < \theta < \pi$?

(A) g is increasing at an increasing rate.

(B) g is increasing at a decreasing rate.

(C) g is decreasing at an increasing rate.

(D) g is decreasing at a decreasing rate.

13. Which of the following best describes the rate of change of g over the interval $\pi < \theta < \dfrac{3\pi}{2}$?

(A) The rate of change of g is positive and increasing.

(B) The rate of change of g is positive and decreasing.

(C) The rate of change of g is negative and increasing.

(D) The rate of change of g is negative and decreasing.

14. Which of the following best describes the behavior of g over the interval $\dfrac{3\pi}{2} < \theta < 2\pi$?

(A) g is increasing and the graph of g is concave up.

(B) g is increasing and the graph of g is concave down.

(C) g is decreasing and the graph of g is concave up.

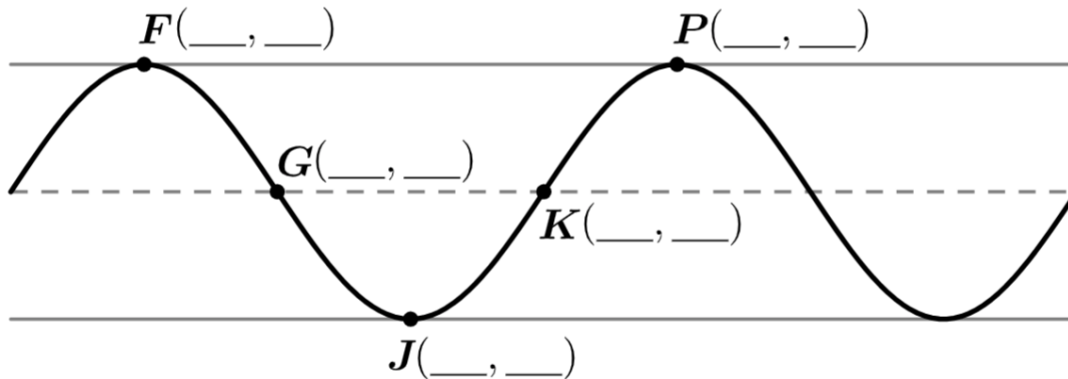(D) g is decreasing and the graph of g is concave down.
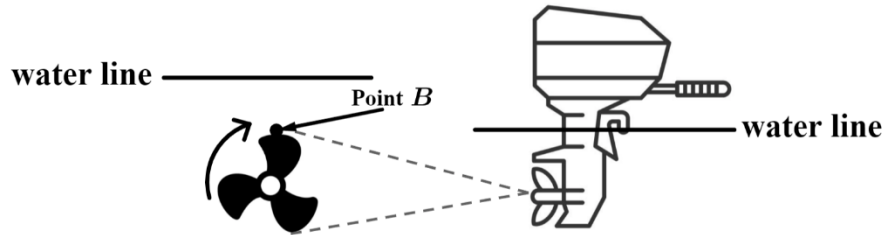
Note: Figure NOT drawn to scale

15. The blades of a boat motor rotate in a clockwise direction and complete 50 rotations every second. Point B is on the tip of one of the blades and is located directly above the center of the motor at time $t = 0$ seconds, as indicated in the figure. Point B is 8 inches from the center of the motor. The center of the motor is 18 inches below the water line. As the blades of the motor rotate at a constant speed, the distance between B and the water line periodically increases and decreases.

The sinusoidal function h models the distance between point B and the water line, in inches, as a function of time t in seconds.

(A) The graph of h and its dashed midline for two full cycles is shown. Five points, $F, G, J, K,$ and P are labeled on the graph. No scale is indicated, and no axes are presented.

Determine possible coordinates $(t, h(t))$ for the five points: $F, G, J, K,$ and P.

(B) Find the period, frequency, amplitude, and midline for the graph of h.

(C) Find two intervals for which the graph of h is both decreasing and concave up.